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( July )

ECONOMICS

( Honours )

## ( Mathematics for Economist )

Marks : 75

Time : 3 hours

The figures in the margin indicate full marks  
for the questions

Answer **five** questions, selecting **one** from each Unit

## UNIT—I

1. (a) Define set. Explain different operations of sets with examples. 2+3=5

(b) Given the sets

$$A \quad \{1, 2, 3, 4\}$$

$$B \quad \{2, 4, 5, 6\}$$

$$C \quad \{0, 3, 4, 7, 8\}$$

Prove the De Morgan's law for union and intersection. 4

- (c) In a class of 25 students of economics and politics, 12 students have taken economics. Out of these 8 have taken economics but not politics. Find the number of students who have taken economics and politics and those who have taken politics but not economics.

$$3+3=6$$

2. (a) Differentiate any *three* of the following with suitable examples : 3×3=9

(i) Linear and quadratic functions

(ii) Homogeneous and homothetic functions

(iii) Explicit and implicit functions

(iv) Domain and range of a function

- (b) Find the equation of the straight line passing through the points (3, -2) and (-4, 1). Also write down the gradient of the line. 4+2=6

## UNIT—II

3. (a) What is matrix? Mention some of its properties. 1+5=6

- (b) Solve the given simultaneous equations by matrix inversion method : 9

$$2x_1 \quad 3x_2 \quad x_3 \quad 15$$

$$4x_2 \quad 2x_3 \quad 16$$

$$3x_1 \quad 2x_2 \quad 18$$

4. (a) State the Hawkins-Simon conditions for input/output analysis. What are its implications? 3+2=5

(b) Prove that  $(ABC)^T = C^T B^T A^T$ . Given

$$A = \begin{pmatrix} 2 & 1 \\ 4 & 2 \end{pmatrix}, B = \begin{pmatrix} 3 & 0 \\ 1 & 5 \end{pmatrix}, C = \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix} \quad 4$$

(c) If

$$A = \begin{pmatrix} 8 & 4 \\ 3 & 7 \end{pmatrix}, B = \begin{pmatrix} 3 & 2 \\ 1 & 5 \end{pmatrix}$$

find the matrix C, such that  $2A + 4B + 3C = 0$ , where 0 is a null matrix. 3

(d) Find the value of k, if A is a singular matrix : 3

$$A = \begin{pmatrix} 2 & 3 & 8 \\ 4 & 5 & k \\ 2 & 2 & 2 \end{pmatrix}$$

UNIT—III

5. (a) Evaluate (any three) : 3×3=9

(i)  $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$

(ii)  $\lim_{x \rightarrow a} \frac{\sqrt{x} - \sqrt{a}}{x - a}$

(iii)  $\lim_{x \rightarrow 1} \frac{5x^3 - 2}{3x^3 - x + 1}$

(iv)  $\lim_{x \rightarrow 2} \frac{x^2 - 6x + 8}{x^2 - 7x + 10}$

(v)  $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{x}$

(b) What makes a function continuous? Given the function

$$f(x) = \begin{cases} 3 - 2x & \text{for } 3/2 \leq x < 0 \\ 3 + 2x & \text{for } 0 \leq x < 3/2 \\ 3 - 2x & \text{for } x \geq 3/2 \end{cases}$$

Is the function continuous at  $x = 0$ ?

2+4=6

6. (a) Differentiate any four of the following functions : 2×4=8

(i)  $y = (2x - 5)(x^2 - x + 1)$

(ii)  $y = (2x^2 - 7)^{10}$

(iii)  $y = \sqrt{x^2 - 5x}$

(iv)  $y = \frac{x^2 - 7}{x^2 + 7}$

(v)  $x^3 - 3xy + 5y - 6 = 0$

(vi)  $y = x^x$

( 5 )

- (b) Find the first- and second-order partial derivatives of the following function :

$$z = 2x^3 + 5x^2y + xy^2 + y^2$$

Verify that

$$\frac{\partial^2 z}{\partial x \partial y} = \frac{\partial^2 z}{\partial y \partial x} \quad 4$$

- (c)  $u = (3x^2 + 5y^2)^5$ . Find  $du$ . 3

UNIT—IV

7. (a) State the necessary and sufficient conditions for maximum and minimum values, and hence find the maximum and minimum values of the function  $y = \frac{1}{3}x^3 + 3x^2 + 8x + 10$ . 2+4=6

- (b) The demand equation for a manufacturer is given by  $P = 500 - 2q$ , and his average cost function is  $0.25q + 4 + \frac{400}{q}$ , where  $q$  is output and  $p$  is price. Determine—  
 (i) the level of output at which profit is maximized;  
 (ii) the price at which this occurs;  
 (iii) the maximum profit. 4+3+2=9

( 6 )

8. (a) The total cost associated with producing and marketing  $x$  units of an item is given by

$$C = 0.005x^3 + 0.02x^2 + 30x + 3000$$

Find AC at 10 units of output and MC at 3 units of output. 3+3=6

- (b) The demand function is given by  $q = \frac{20}{p + 3}$ . Calculate price elasticity of demand at price  $p = 2$  and also interpret the result. 7+2=9

UNIT—V

9. (a) What is integration? Why is there a constant of integration? 1+2=3
- (b) Find the integral of the following (any four) : 3×4=12

(i)  $\int (4x^3 + \frac{1}{\sqrt{x}} + 3) dx$

(ii)  $\int 4(e^{2x} - x)(e^{2x} + x^2)^2 dx$

(iii)  $\int \frac{8x}{(2x^2 + 1)} dx$

(iv)  $\int x^2 e^x dx$

(v)  $\int x \log x dx$

(vi)  $\int 10^{-x} dx$

10. (a) Evaluate : 3

$$\int_2^4 3x^2(x^2 - 1) dx$$

(b) What is producer's surplus? If the production function is given by  $Q = \sqrt{4 - 4p}$  and the market price is 10, find the producer's surplus. 2+4=6

(c) The demand and supply functions are  $P_d = (6 - q)^2$  and  $P_s = 14 - q$  respectively. Find the consumer's surplus under perfect competition. 6

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